

can again compute the "excess" value of bids. The dual variables  $\lambda_p$  associated with the players also play a role in the generation of proposals. Since we can select only one proposal per player, and a large dual variable, would indicate that there are many "good" proposals for that player already being considered, we should give preference to players from whom the dual variable is small. Linear programming theory says that a proposals C for player p can increase the objective function value of the linear programming relaxation of the integer program if and only if

**IN THE CLAIMS:**

**Please amend the claims to read as follows:**

1. (Amended) A method for executing a combinatorial auction, the method comprising:
- (1) reading input data comprising:
    - (i) items;
    - (ii) player bidding on the items; and
    - (iii) bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;
  - (2) generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction;
  - (3) selecting a set of proposals such that each items is included in at most one selected proposal;
  - and
  - (4) informing the players bidding on the items of the result of said selecting a set of proposals.
2. (Amended) A method according to claim 1, wherein said reading input data comprises reading input data further including at least one type that is specified for each bid, and wherein said generating proposals are limited to collections of bids from a player that are

of the same type, and wherein said selecting a set of proposals is limited to sets that include at most one proposal for each player.

3. (Amended) A method according to claim 1, wherein said generating proposals comprises generating all possible proposals.

*Int B3*  
4. (Amended) A method according to claim 1, wherein said selecting a set of proposals is enabled by using an integer programming technique.

5. (Amended) A method according to claim 1, wherein said selecting a set of proposals comprises selecting a set of proposals that maximizes the total value of the bids included in the selected proposals.

*Int B3*  
6. (Amended) A method for selecting a set of bids in a combinatorial auction for at least two items involving at least one player and at least one type of bid for each player such that:

(a) each item is contained in at most one (or exactly one) selected bid;

(b) for each player, the selected bids all belong to the same type;

and among all collections of bids satisfying (a) and (b) the selected bids maximizing total revenue, said method comprising:

(1) generating all valid proposals;

(2) formulating an integer program that includes a column for each proposal, a constraint for each item and a constraint for each player, said constraints representing conditions (a) and (b) respectively, and an objective function which represents revenue;

(3) solving the integer program for selecting the set of proposals that maximizes revenue;

and

(4) constructing a set of winning bids from the set of winning proposals.

7. (Amended) A method according to claim 6, further comprising checking for ties by

adding a constraint.

*Def B4*  
8. (Amended) A method for selecting a set of bids in a combinational auction for at least two items involving at least one player and at least one type of bid for each player such that:

(a) each item is contained in at most one (or exactly one) selected bid;

(b) for each player, the selected bids all belong to the same type;

and among all collection of bids satisfying (a) and (b) the selected bids maximizes total revenue, said method comprising:

*A3*  
(1) generating a set of valid proposals;

(2) formulating an integer program that includes a column for each proposal, a constraint for each item and a constraint for each player, said constraint representing conditions (a) and (b) respectively, and an objective function which represents revenue;

(3) solving a linear programming relaxation of the integer program in said formulating an integer program for obtaining dual variables associated with each of the constraints;

(4) using dual variables obtained in said solving a linear programming relaxation for determining the excess value associated with each bid, and a threshold for each player;

(5) using a proposal generation method for selecting each player and type, a proposal for which the excess value exceeds the threshold, or determining that no such proposal exists;

(6) adding the proposal generated in said using a proposal generation method and repeating said solving a linear programming relaxation, said using dual variables, and said using a proposal generation method until no new proposals are identified;

(7) solving the integer program that includes all identified proposals; and

(8) constructing a set of winning bids from the set of winning proposals.

9. (Amended) A program storage device readable by a machine, tangibly embodying a program of instructions executable by the machine to perform method steps for executing a combinatorial auction, said method steps comprising:

(1) reading input data comprising:

- (i) items;
- (ii) players bidding on the items;

and (iii) bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;

(2) generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction;

(3) selecting a set of proposals such that each item is included in at most one selected proposal; and

(4) informing the players bidding on the items of the results in said selecting a set of proposals.

10. (Amended) A computer comprising:

(1) means for reading input data comprising:

- (i) item;
- (ii) players bidding on the items; and

(iii) bids, where each bid specifies the player bidding, the amount bid, and the list of items included in the bid;

(2) means for generating proposals by utilizing the input data, each said proposal comprising a collection of bids that can be awarded to a player participating in the auction;

(3) means for selecting a set of proposals such that each item is included in at most one selected proposal;

(4) means for informing the players bidding on the items of the results in said means for selecting.

**Please add the following new claims:**

11. The method of claim 1, wherein:

said selecting a set of proposals comprises constructing a constraint matrix, wherein the

matrix has a row for each player, a row for each item, and a column for each of the proposals;  
formulating an integer program from the matrix;  
solving the integer program with a subset of proposals from the matrix;  
creating a new proposals subset by adding proposals to the proposal subset if adding proposals to the subset will optimize the solution;  
solving the integer program using the new proposal subset;  
repeating the adding of proposals and the solving of the integer program until an optimal solution is determined.

12. The method of claim 11, wherein said adding proposals to the proposal subset comprises using a proposal generation to generate the addition proposals until an optimal solution to the integer program is determined.

13. The method of claim 6, wherein said solving the integer program comprises solving the integer program with a subset of proposals, said method further comprising:

ay creating a new proposals subset by adding proposals to the proposal subset if adding proposals to the subset will optimize the solution;  
solving the integer program using the new proposal subset;  
repeating the adding of proposals and the solving of the integer program and until an optimal solution is determined.

14. The method of claim 13, wherein said adding proposals to the proposal subset comprises using proposal generation methods to generate the addition proposals until an optimal solution to the integer program is determined.

15. The method of claim 8, wherein the using of a proposal generation method comprises adding randomly generated proposals to the integer program.

16. The method of claim 8, wherein the using of a proposal generation method comprises using a branch-and-bound method to search for additional proposals which, if added to the integer program, will optimize the solution.

17. The program storage device of claim 9, wherein the generating of a set of proposals comprises constructing a constraint matrix, wherein the matrix has a row for each player, a row for each item, and a column for each of the proposals, said device further comprising:

formulating an integer program from the matrix;  
solving the integer program with a subset of proposals from the matrix;  
creating a new proposals subset by adding proposals to the proposal subset if adding proposals to the subset will optimize the solution;  
solving the integer program using the new proposal subset; and  
repeating the steps of adding proposals and solving the integer program and until an optimal solution is determined.

18. The program storage device of claim 17, wherein:

step (2) for generating proposals comprises adding randomly generated proposals to the integer program.

19. The computer of claim 10, wherein:

means for generating a set of proposals comprises creating a new proposals subset by adding proposals to the proposal subset if adding proposals to the subset will optimize the means for selecting a set of proposals.

20. The method according to claim 6, wherein:

the subsets of new proposals obey the constraints within the integer program.

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